

Szabadformájú alakzatok tervezése poliéderek segítségével

Szörfi Jázmin

Konzulens: Várady Tamás

3D számítógépes geometria 2 - 2020



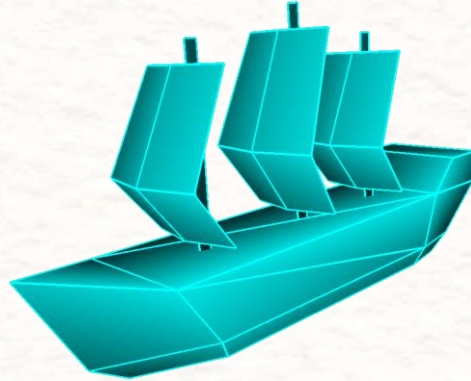
Tartalom

- Kontrollpoliéder alapú tervezés
- GB-patch
- Kétfajta reprezentáció bemutatása
- Algoritmus
 - Görbeháló struktúrák
 - Sima kapcsolódás
- Tesztprogram

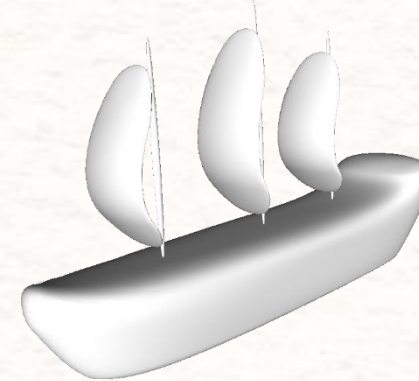
Kontrollpoliéder alapú tervezés



Hajó(x,y,z) = ?

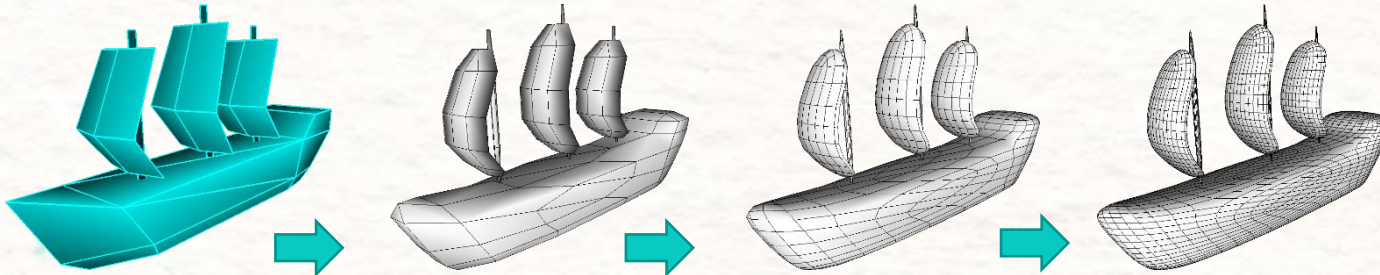


Kontrollpoliéder

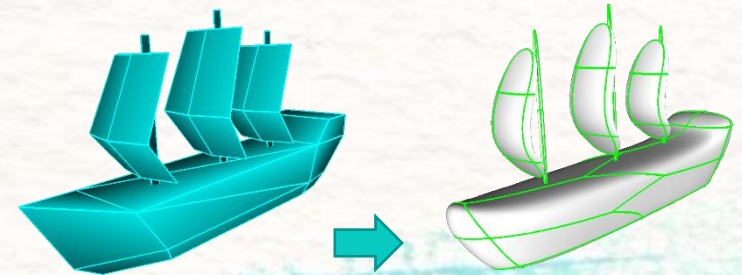


Felület

Rekurzív felosztás



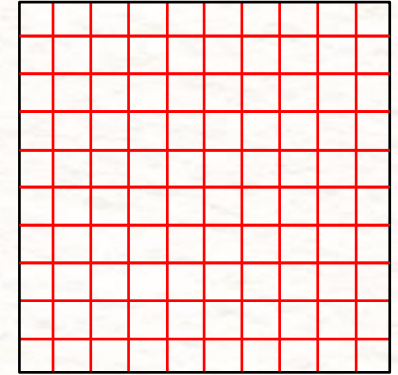
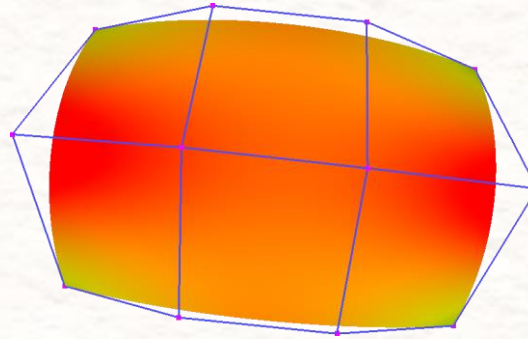
Görbeháló interpoláció



N-oldalú Bézier-felületek

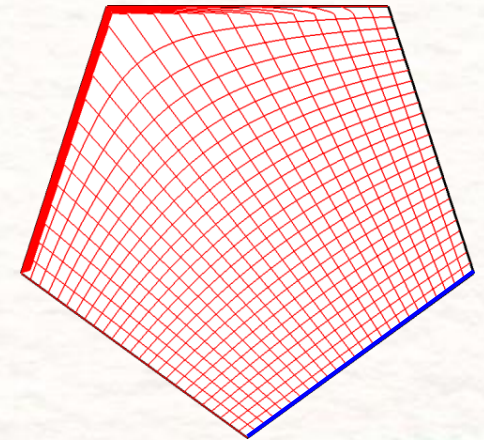
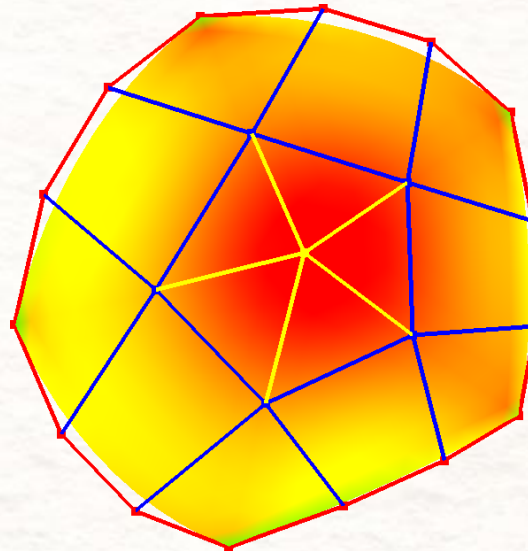
Hagyományos reprezentáció

- Négy oldalú domén
- Szabályos kontrollrács

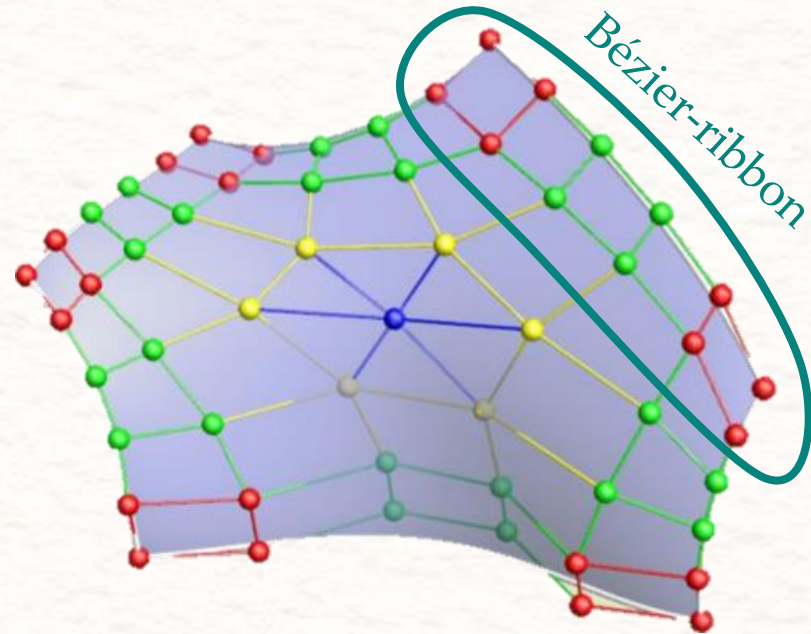


GB-patch reprezentáció

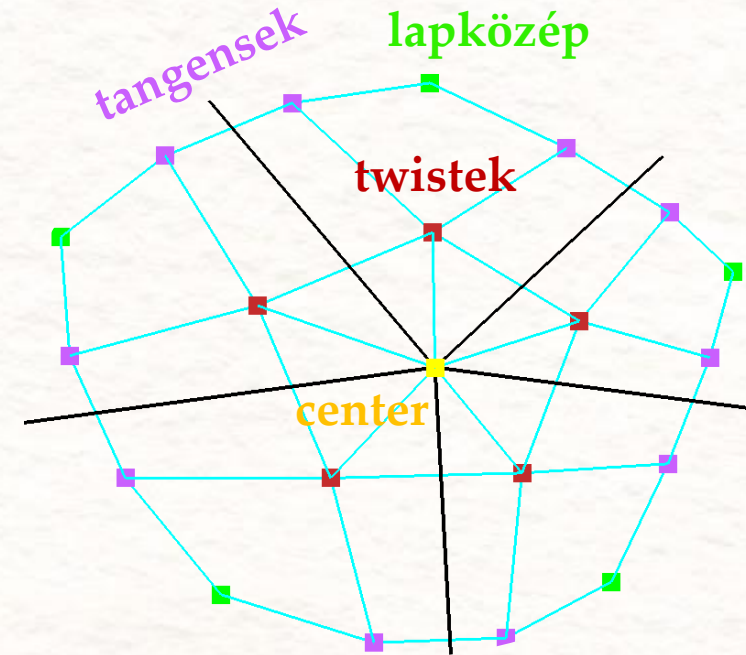
- N-oldalú domén
- Speciális paraméterezés
- Általános kontrollstruktúra



GB kontrollpont háló

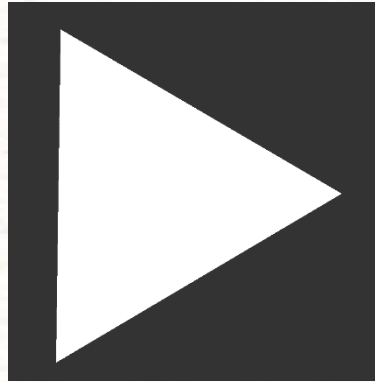


- **sarok kontrollpontok:**
- **ribbon kontrollpontok:**
- **belső kontrollpontok:**
- **középső kontrollpont:**

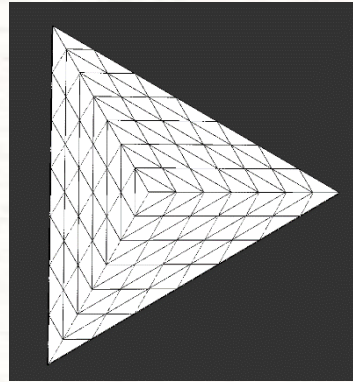


az i -edik és az $(i+1)$ -edik oldalhoz is tartoznak
csak az i -edik oldalhoz tartoznak
fokszámemelés által keletkeznek
csak a felület belsejére hat

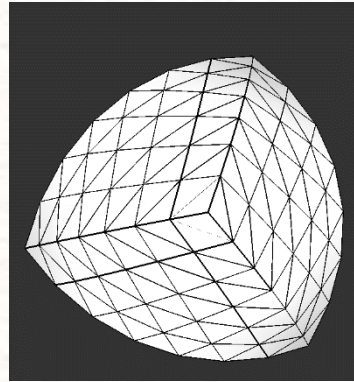
GB domén, általános baricentrikus koordináták



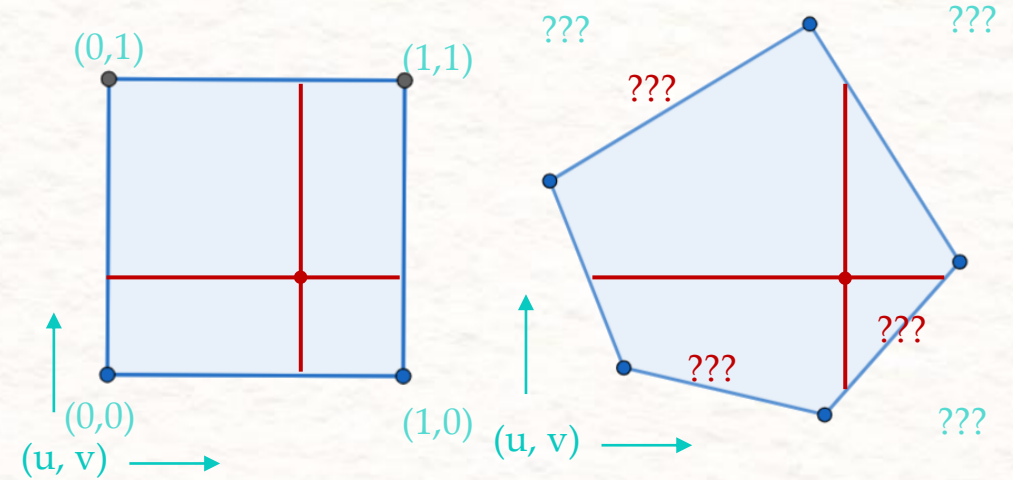
Domain



Felosztás



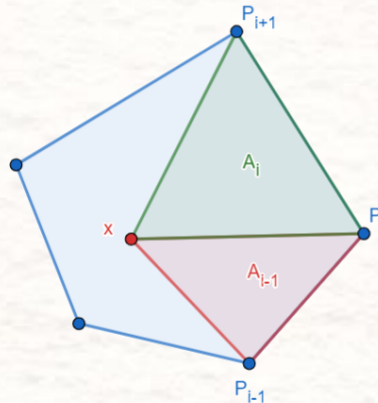
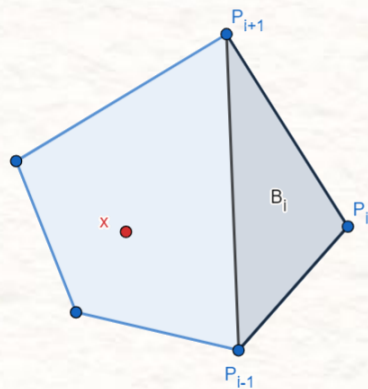
Felület



Általános baricentrikus koordináták

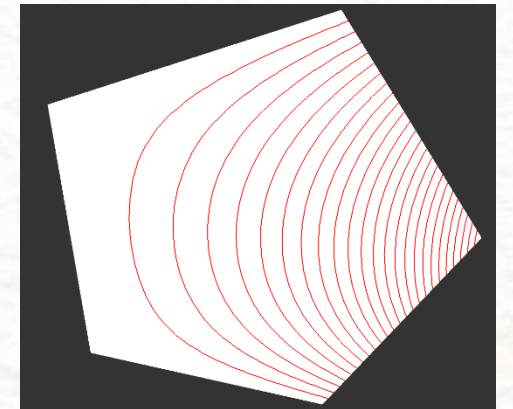
$$\mathbf{X} = \sum_{i=1}^n \lambda_i(\mathbf{X}) \mathbf{P}_i$$

$$\sum_{i=1}^n \lambda_i(\mathbf{X}) = 1$$



$$w_i(\mathbf{X}) = \frac{B_i}{A_{i-1} A_i}$$

$$\lambda_i(\mathbf{X}) = \frac{w_i(\mathbf{X})}{\sum_{j=1}^n w_j(\mathbf{X})}$$

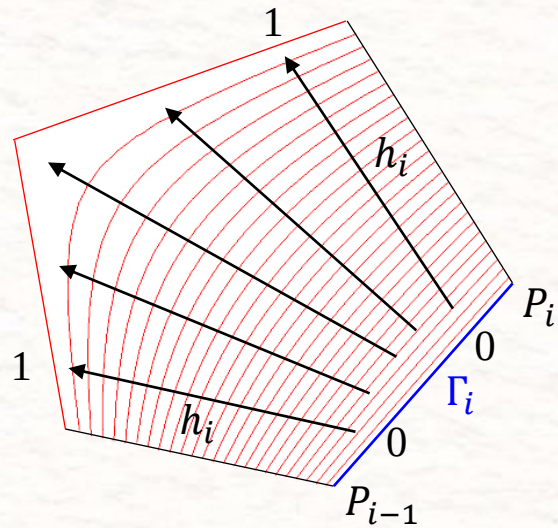


λ_i szintvonalak

Lokális paraméterek és felület

Távolságparaméter

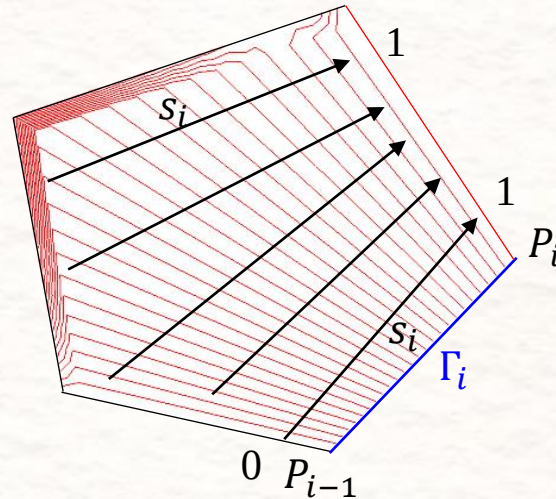
$$h_i = 1 - \lambda_{i-1} - \lambda_i$$



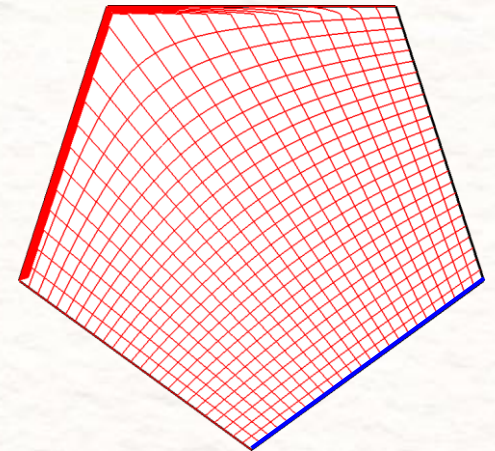
+

Oldalparaméter

$$s_i = \frac{\lambda_i}{\lambda_{i-1} + \lambda_i}$$



=



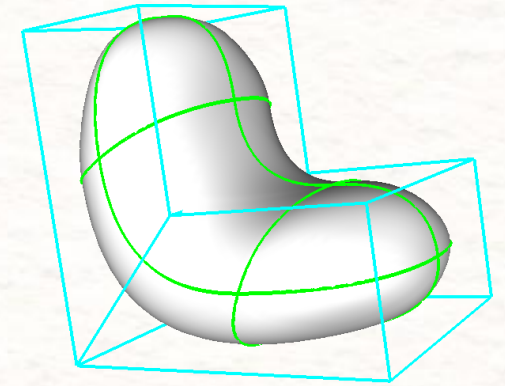
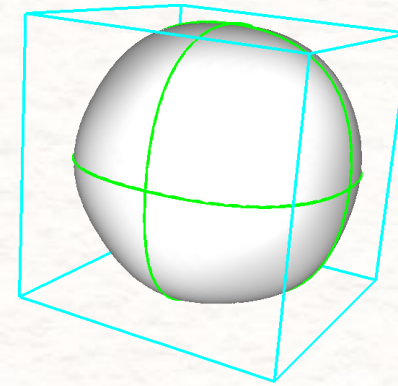
Lokális paraméterek + kontroll pontok $\rightarrow$ felület egyenlete:

$$S(u, v) = \sum_{i=0}^{n-1} \sum_{j=0}^d \sum_{k=0}^{l-1} C_{j,k}^{d,i} \mu_{j,k}^i B_{j,k}^d(s_i(u, v), h_i(u, v)) + C_0 B_0(u, v) \quad B_0: \text{konvex kombináció biztosítása}$$

Két görbeháló struktúra

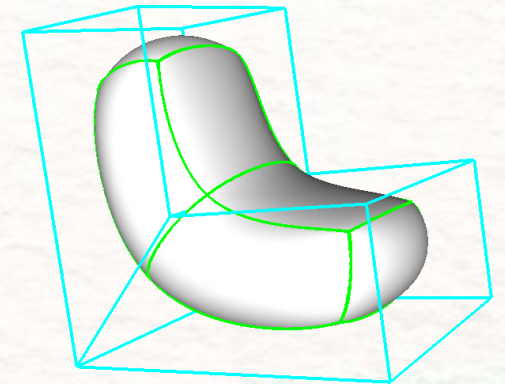
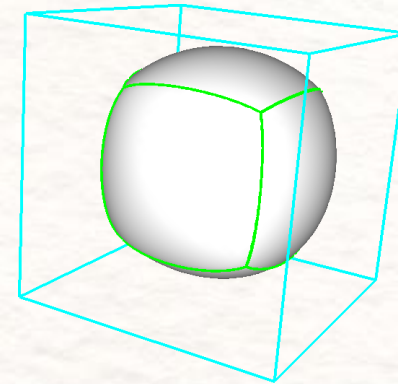
Duális:

- Patch oldalszáma $\sim$ csúcs fokszáma
- Csak konvex lapok
- Generalised Bézier (GB) patch reprezentáció
- Állítható görbültségi paraméter: induló tangens

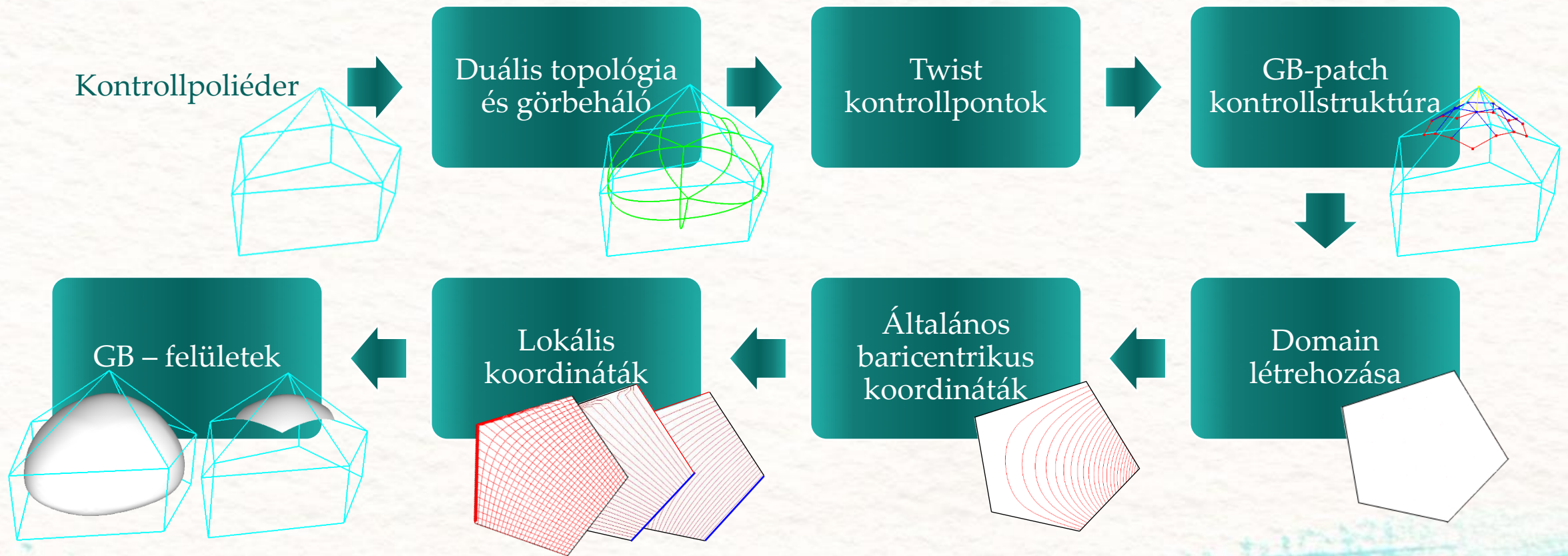


Topológia tartó:

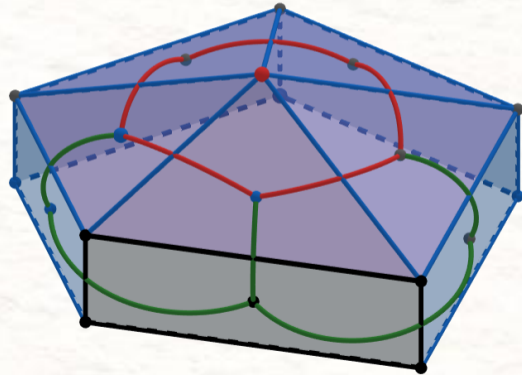
- Patch oldalszáma $\sim$ lap oldalszáma
- Konvex, konkáv és lyukas lapok (végső cél)
- Concave GB (CGB) patch reprezentáció
- Állítható görbültségi paraméter: lapkamélység



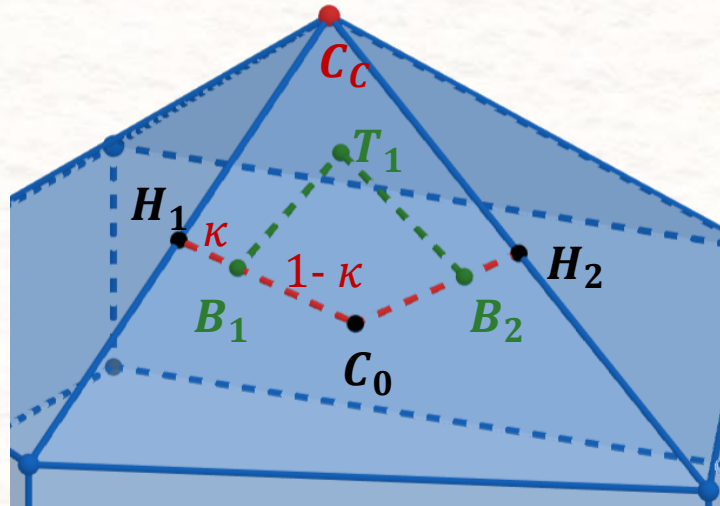
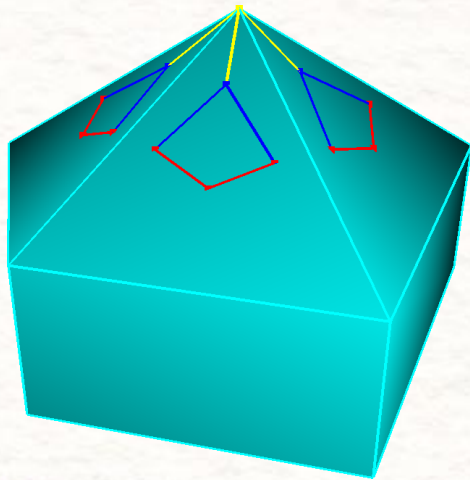
A duális algoritmus blokkdiagramja



Duális topológia, kontrollpontok



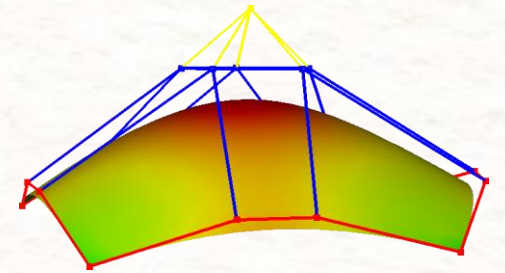
Duális topológia



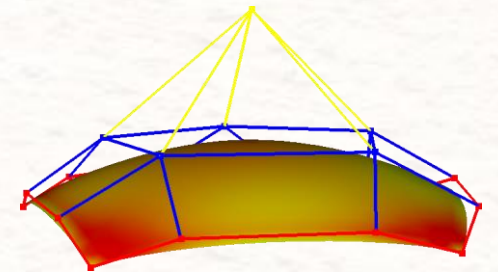
$$B_1 = \kappa C_0 + (1 - \kappa) H_1$$

$$B_2 = \kappa C_0 + (1 - \kappa) H_2$$

$$T_1 = \kappa^2 C_0 + \kappa(1 - \kappa) H_1 + \kappa(1 - \kappa) H_2 + (1 - \kappa)^2 C_c$$

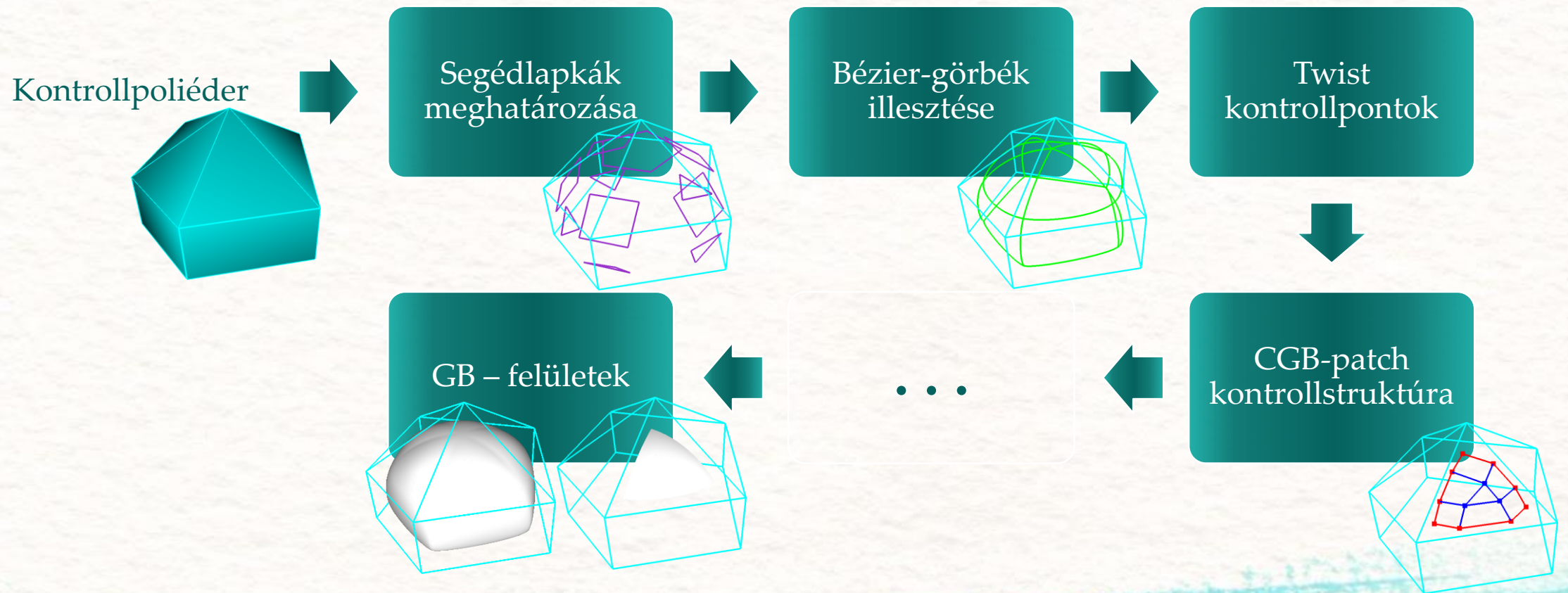


Nagy induló tangens

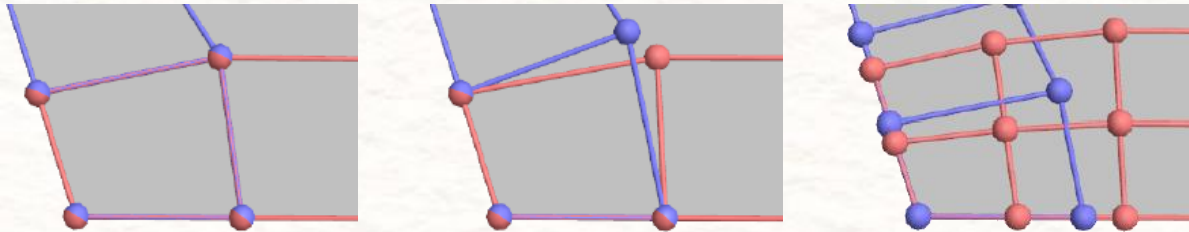
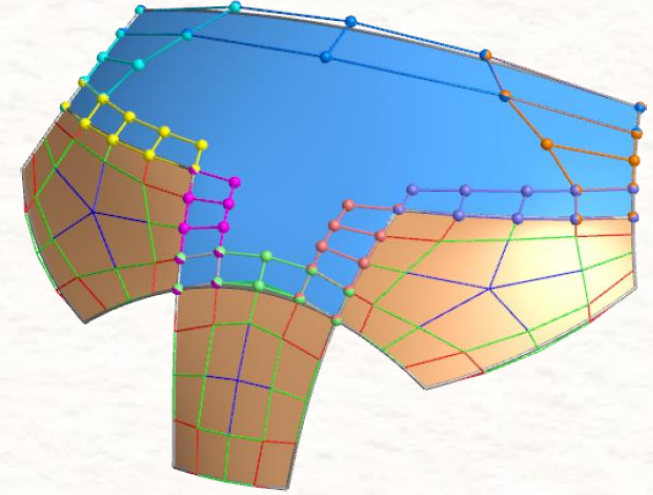
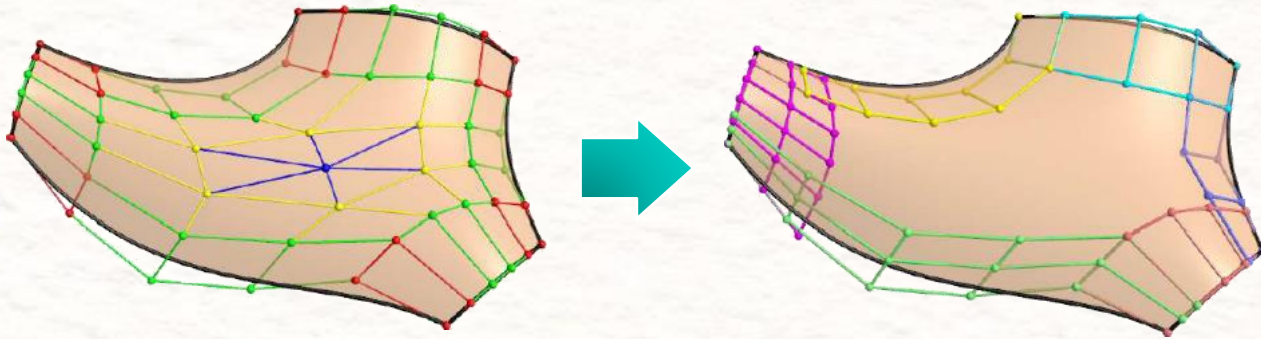


Kis induló tangens

A topológiatartó algoritmus blokkdiagramja



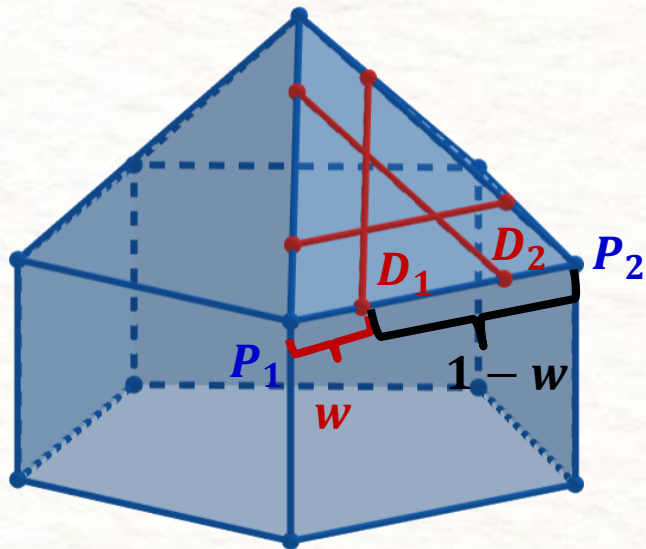
Konkáv GB-patch reprezentáció



$$S(u, v) = \frac{1}{B_{sum}(u, v)} \sum_{i=0}^n \sum_{j=0}^{d_i} \sum_{k=0}^{l_i-1} C_{j,k}^i \mu_{j,k}^i B_{j,k}^{d_i}(s_i(u, v), h_i(u, v))$$

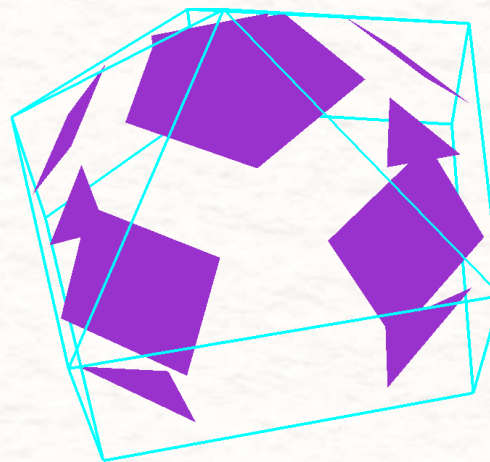
B_{sum} : konvex kombináció biztosítása

Segédlapkák létrehozása

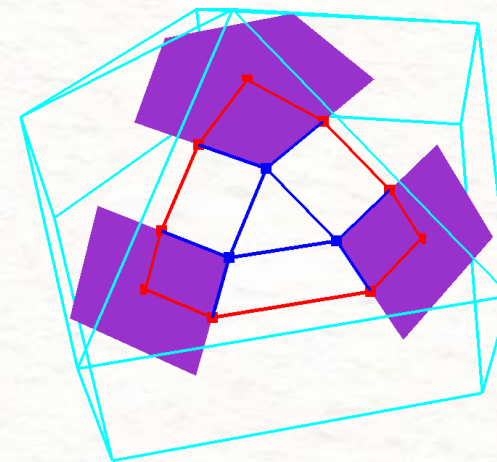


$$D_1 = w P_2 + (1 - w) P_1$$

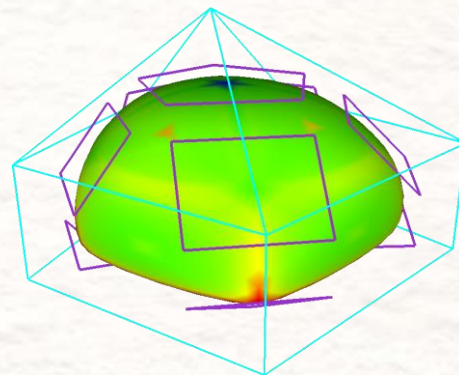
$$D_2 = w P_1 + (1 - w) P_2$$



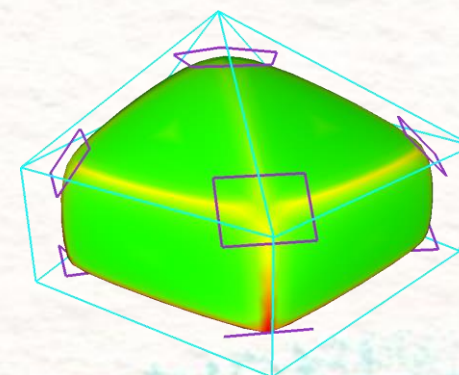
Segédlapkák



Kontrollpontok



Nagy segédlapkák



Kis segédlapkák

Sima kapcsolódás - csúcsokban

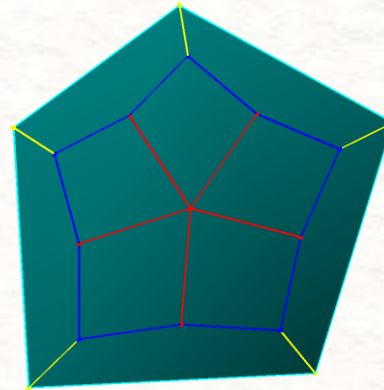
Közös érintősík a csúcsokban

Duális

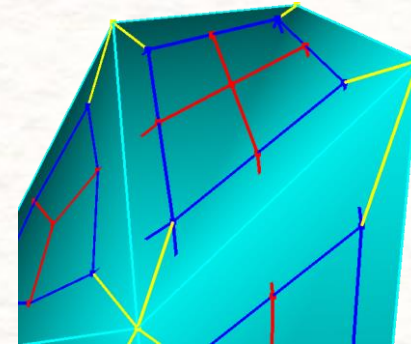
- Síklap ✓
- 3 (síklap) vagy 4 befutó él ✓

Topológiatartó

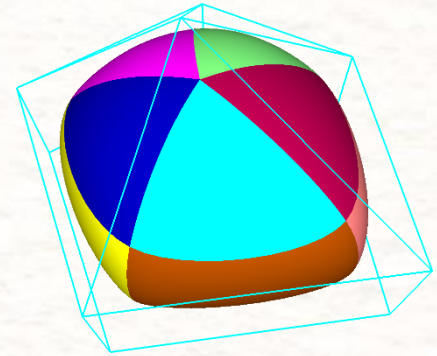
- 3 befutó él ✓



Síklap



4 befutó él

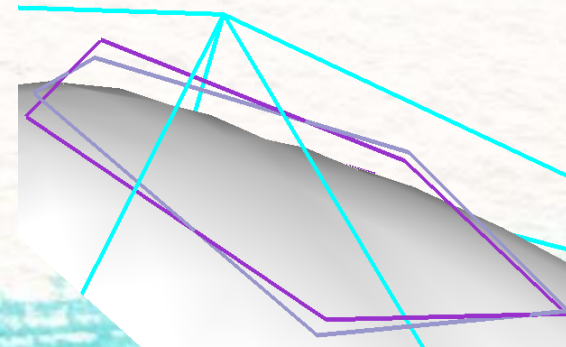
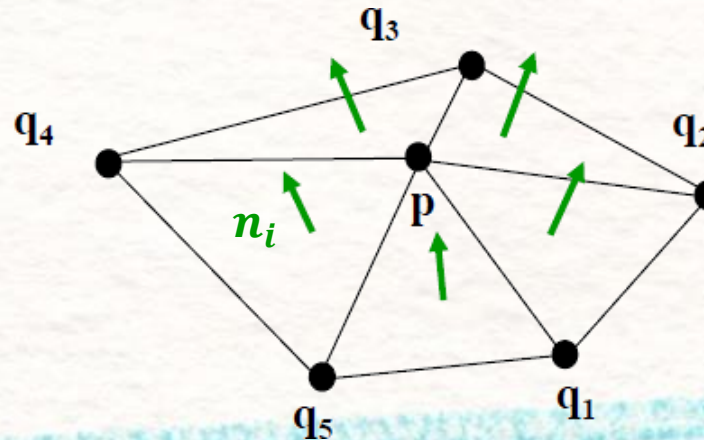


Legjobb négyzetes sík

$$\mathbf{n}_i = (\mathbf{q}_i - \mathbf{p}) \times (\mathbf{q}_{i+1} - \mathbf{p})$$

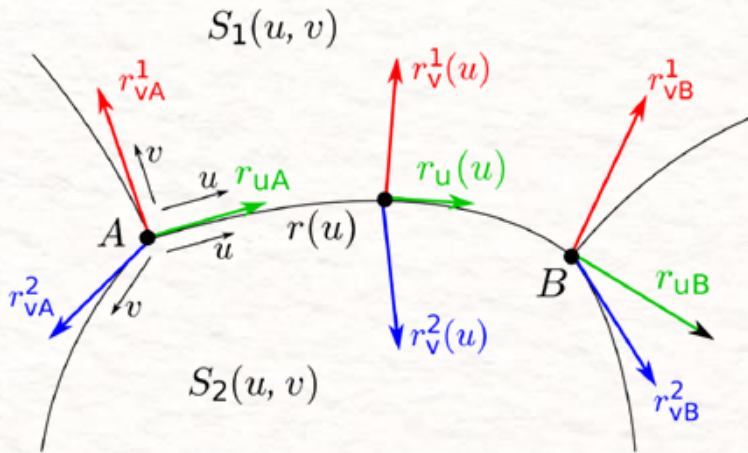
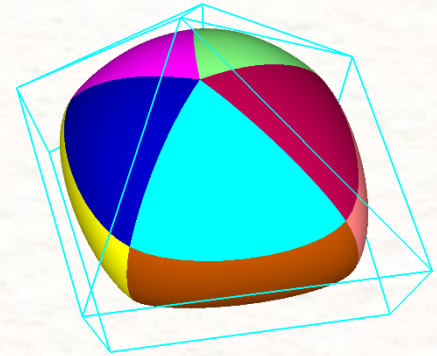
$$A = \frac{1}{2} \sum_i |\mathbf{n}_i|$$

$$\mathbf{n}_p = \frac{1}{2A} \sum_i \mathbf{n}_i$$



Sima kapcsolódás – élek mentén

Közös irányblend – közös érintő sík az él mentén



$$N_1(u) = \dot{\mathbf{r}}_u(u) \times \dot{\mathbf{r}}_v^1 u$$

$$N_2(u) = \dot{\mathbf{r}}_u(u) \times \dot{\mathbf{r}}_v^2 u$$

$$\mathbf{r}_v^i(u) = \alpha^i(u)\mathbf{D}(u) + \beta^i(u)\mathbf{r}_u(u)$$

$$\alpha(u) = (1 - u)\alpha_A + u\alpha_B$$

$$\beta(u) = (1 - u)\beta_A + u\beta_B$$

Széleken eredeti deriváltak:

$$\mathbf{r}_v^i(0) = \mathbf{r}_{vA}^i$$

$$\mathbf{r}_v^i(1) = \mathbf{r}_{vB}^i$$

Szélső blend értékek:

$$\mathbf{D}(0) = \mathbf{D}_0 = \frac{\mathbf{r}_{vA}^1 - \mathbf{r}_{vA}^2}{2}$$

$$\mathbf{D}(1) = \mathbf{D}_1 = \frac{\mathbf{r}_{vB}^1 - \mathbf{r}_{vB}^2}{2}$$

Approximáló irányblend

D_0 , D_1 és $D_{0.5}$

$D(u)$ közelítse (approximálja) $D_{0.5}$

$$D(u) = (1 - u)^2 D_0 + 2u(1 - u) D_{0.5} + u^2 D_1$$

$$D(u)\alpha(u) = \sum_{i=0}^3 B_i^3(u) Q_i^\alpha$$

$$D(u)\alpha(u) = (1 - u)^3 \alpha_A D_A + 3u(1 - u)^2 \frac{2\alpha_A D_{0.5} + \alpha_B D_A}{3} + 3u^2(1 - u) \frac{\alpha_A D_B + 2\alpha_B D_{0.5}}{3} + u^3 \alpha_B D_B$$

$$C_{i,1} = C_{i,0} + \frac{Q_i}{3}$$

u	D_0	$D_{0.5}$	D_1
0	1	0	0
0.5	1/4	1/2	1/4
1	0	0	1

Interpoláló irányblend

$$\mathbf{D}(0.5) = \mathbf{D}_{0.5}$$

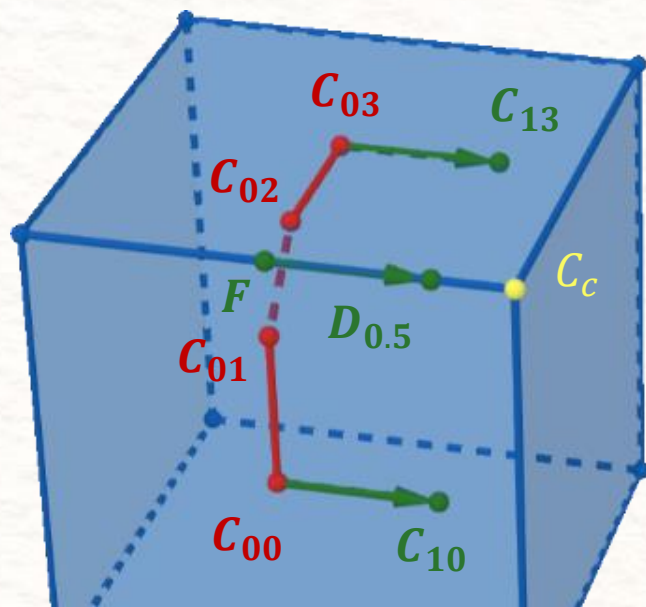
$$\mathbf{D}(u) = (2u^2 - 3u + 1)\mathbf{D}_0 + 4u(1 - u)\mathbf{D}_{0.5} + (2u^2 - u)\mathbf{D}_1$$

u	$\mathbf{D}_0$	$\mathbf{D}_{0.5}$	$\mathbf{D}_1$
0	1	0	0
0.5	0	1	0
1	0	0	1

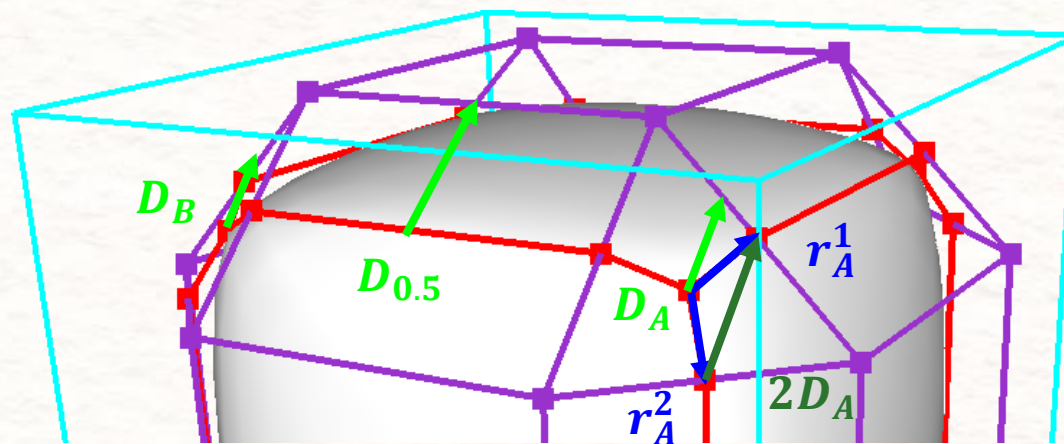
$D_{0.5}$ választása

Duális

$$D_{0.5} = 3(\kappa F + (1 - \kappa) C_c)$$



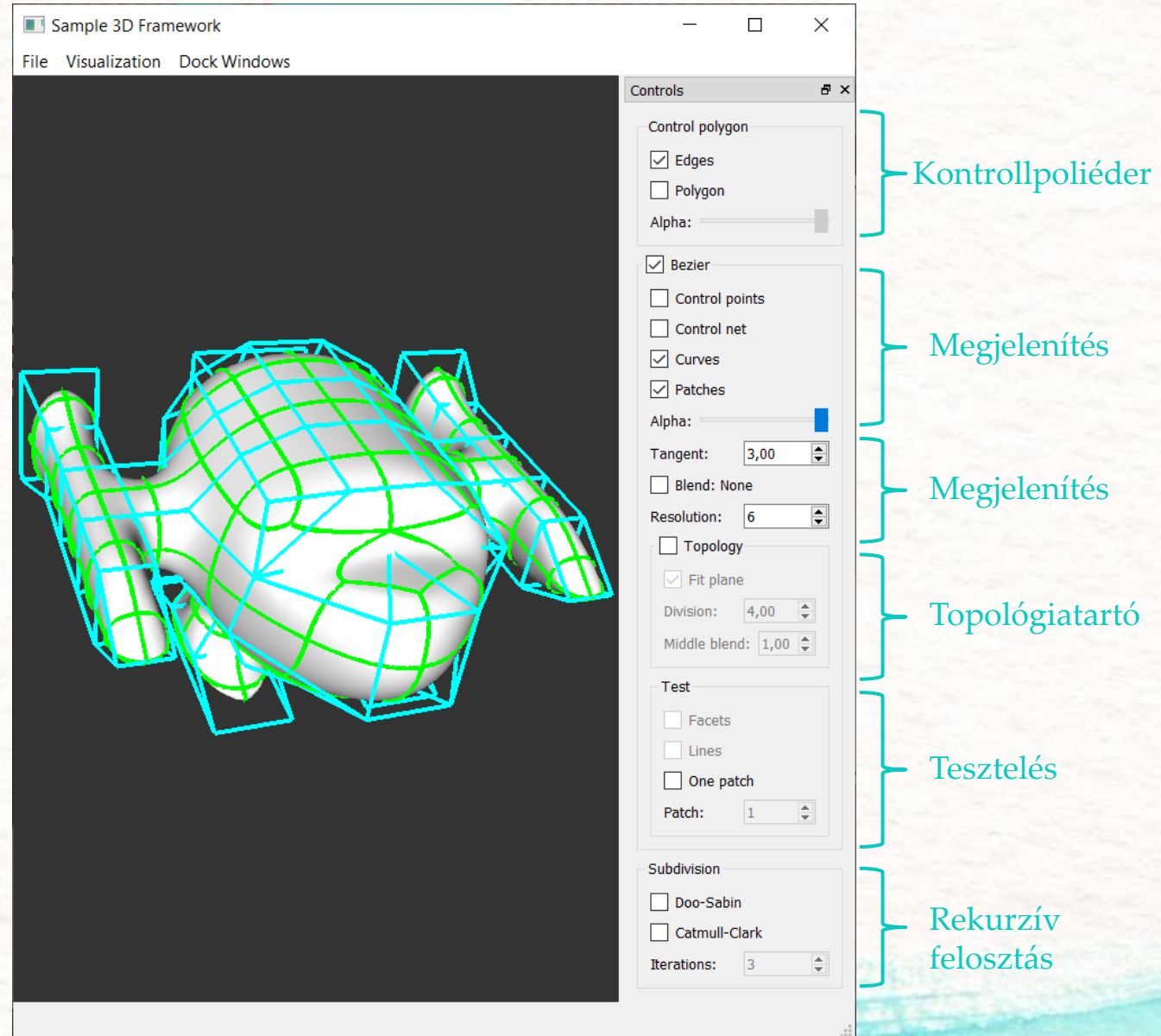
Topológiatartó



Tesztprogram

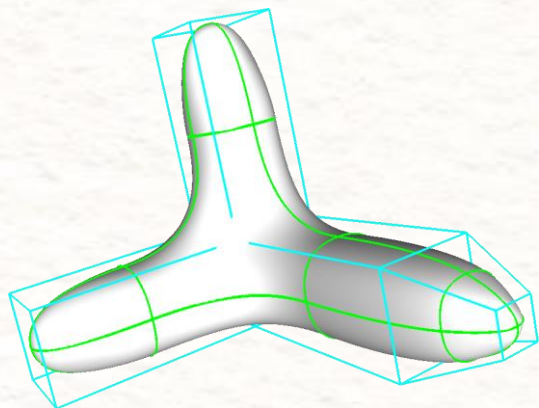
- Futtató környezet – Sample Framework*
 - OpenMesh
 - OpenGL
 - C++
- UI kiegészítés (Qt)
- Mesh kezelés
 - .obj beolvasás
 - Navigálás
 - Számítások

*<https://github.com/salvipeter/sample-framework>

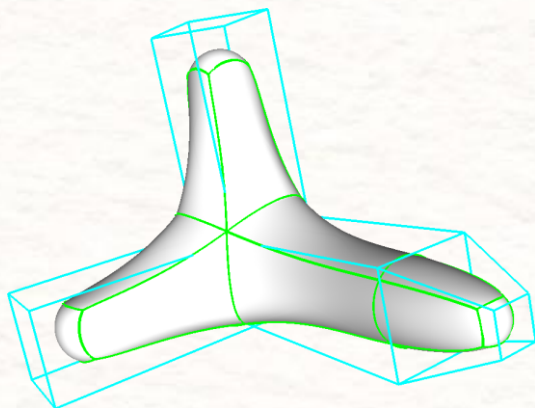


Tesztpéldák

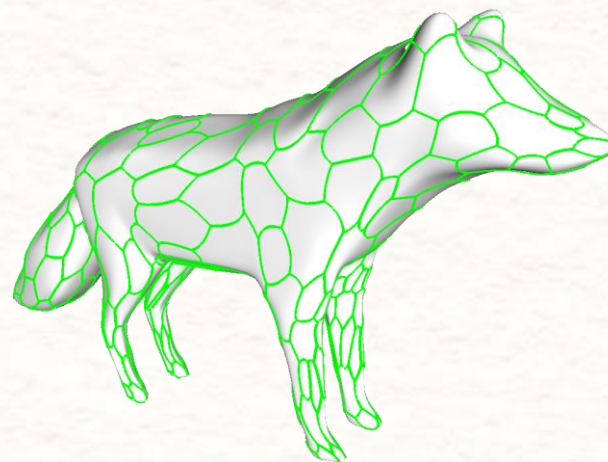
Duális



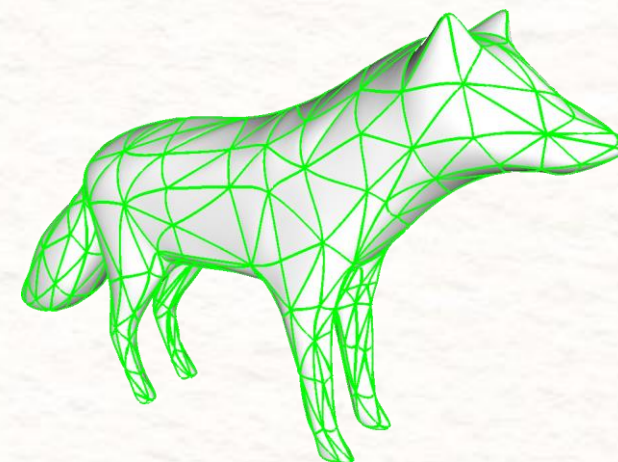
Topológiatartó



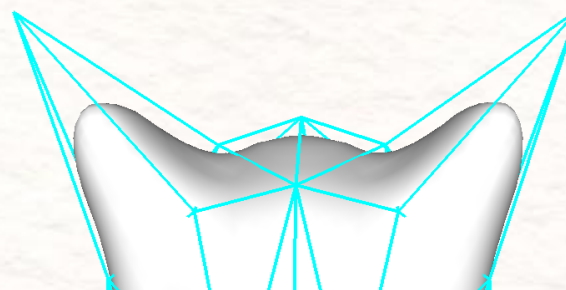
Duális



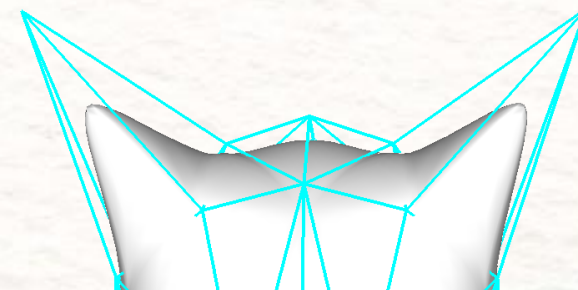
Topológiatartó



Görbeháló



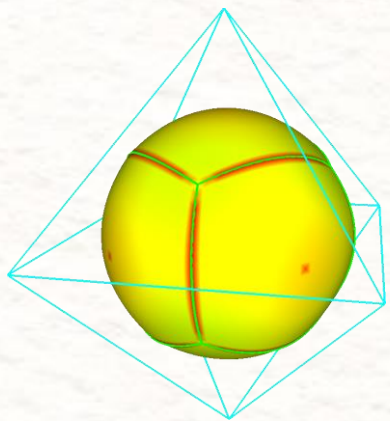
Görbeháló



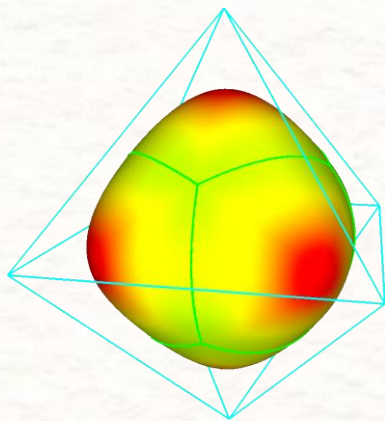
Lekerekítés

Csúcsosság megőrzése

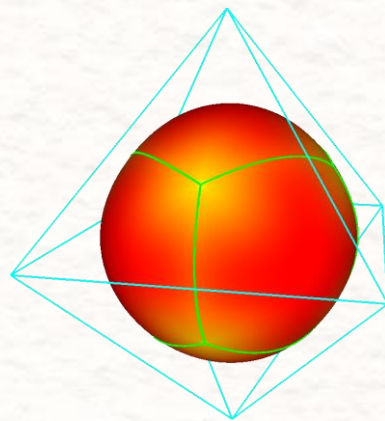
Tesztpéldák



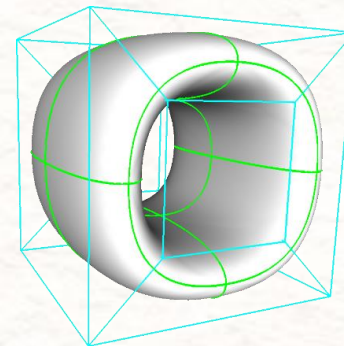
Blend nélkül



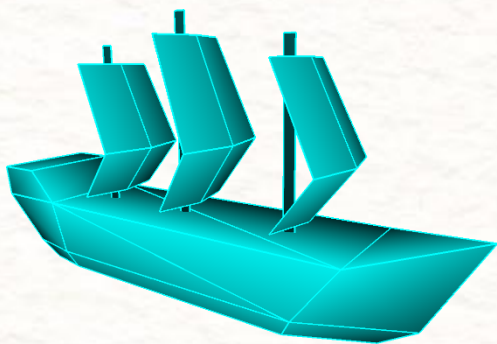
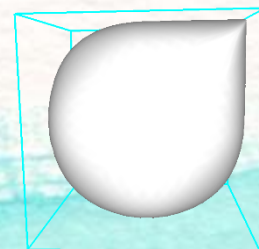
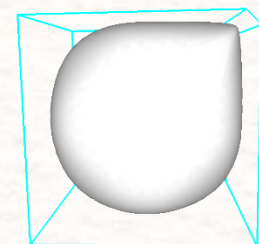
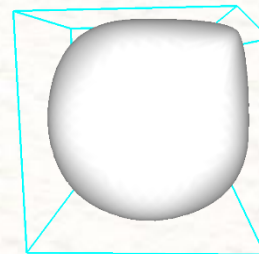
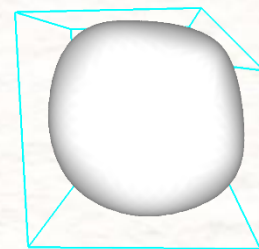
Interpoláló



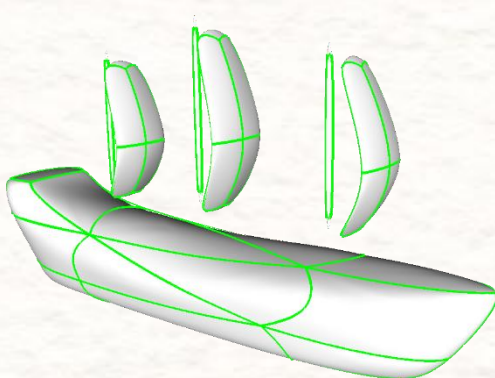
Approximáló



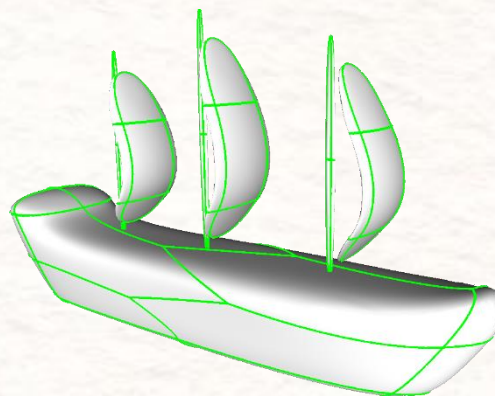
Duális



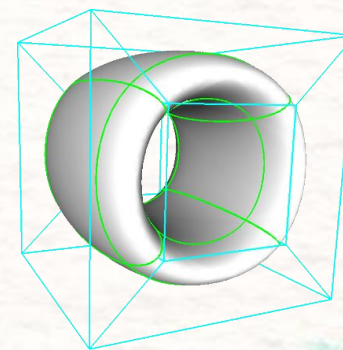
Kontrolpoliéder



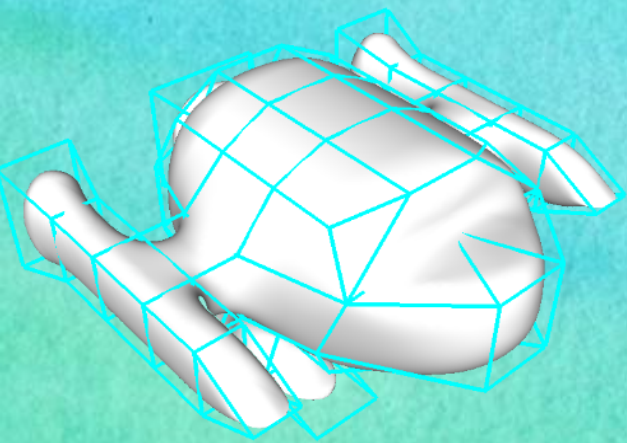
Duális



Topológia tartó



Topológia tartó



Köszönöm a figyelmet!

